



Great Idea #1: Abstraction (Levels of Representation/Interpretation)

C Program

```
int square(int num) {
return num * num;
}
```

Binary

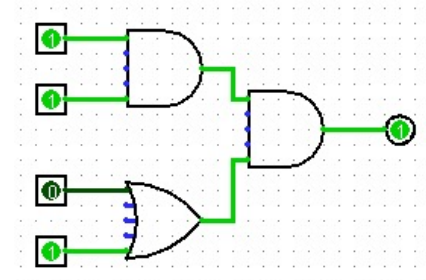
```
0x00000317
0x00830067
0xff010113
0x00112623
0x00812423
0x01010413
0xfea42a23
.....
```

Assembly

square(int):

```
addi    sp, sp, -16
sw       ra, 12(sp)
sw       s0, 8(sp)
addi     s0, sp, 16
sw       a0, -12(s0)
lw       a0, -12(s0)
mul      a0, a0, a0
lw       s0, 8(sp)
lw       ra, 12(sp)
addi     sp, sp, 16
ret
```

Logic



Binary and Hexadecimal

❖ Binary is base 2

- Symbols: 0, 1
- Convention: $2_{10} = 10_2 = 0b10$

❖ Example: What is 0b110 in base 10?

- $0b110 = 110_2 = (1 \times 2^2) + (1 \times 2^1) + (0 \times 2^0) = 6_{10}$

❖ Hexadecimal (**hex**, for short) is base 16

- Symbols? 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, **A, B, C, D, E, F**
- Convention: $16_{10} = 10_{16} = 0x10$

❖ Example: What is 0xA5 in base 10?

- $0xA5 = A5_{16} = (10 \times 16^1) + (5 \times 16^0) = 165_{10}$

Base Comparison

- ❖ Why does all of this matter?
 - *Humans* think about numbers in **base 10**, but *computers* “think” about numbers in **base 2**
 - **Binary encoding** is what allows computers to do all of the amazing things that they do!
- ❖ You should have this table memorized by the end of the class
 - Might as well start now!

Base 10	Base 2	Base 16
0	0000	0
1	0001	1
2	0010	2
3	0011	3
4	0100	4
5	0101	5
6	0110	6
7	0111	7
8	1000	8
9	1001	9
10	1010	A
11	1011	B
12	1100	C
13	1101	D
14	1110	E
15	1111	F

Numerical Encoding

❖ **AMAZING FACT: You can represent *anything* countable using numbers!**

- Need to agree on an **encoding**
- Kind of like learning a new language

❖ Examples:

- Decimal Integers: $0 \rightarrow 0b0$, $1 \rightarrow 0b1$, $2 \rightarrow 0b10$, etc.
- English Letters: CSE $\rightarrow 0x435345$, yay $\rightarrow 0x796179$
- Emoticons: 😊 0x0, 😞 0x1, 😎 0x2, 😇 0x3, 😈 0x4, 🙋 0x5

Binary Encoding – Characters/Text

❖ ASCII Encoding (www.asciitable.com)

■ American Standard Code for Information Interchange

Dec	Hx	Oct	Char	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr
0	0	000	NUL (null)	32	20	040	 	Space	64	40	100	@	@	96	60	140	`	`
1	1	001	SOH (start of heading)	33	21	041	!	!	65	41	101	A	A	97	61	141	a	a
2	2	002	STX (start of text)	34	22	042	"	"	66	42	102	B	B	98	62	142	b	b
3	3	003	ETX (end of text)	35	23	043	#	#	67	43	103	C	C	99	63	143	c	c
4	4	004	EOT (end of transmission)	36	24	044	$	\$	68	44	104	D	D	100	64	144	d	d
5	5	005	ENQ (enquiry)	37	25	045	%	%	69	45	105	E	E	101	65	145	e	e
6	6	006	ACK (acknowledge)	38	26	046	&	&	70	46	106	F	F	102	66	146	f	f
7	7	007	BEL (bell)	39	27	047	'	'	71	47	107	G	G	103	67	147	g	g
8	8	010	BS (backspace)	40	28	050	(	(	72	48	110	H	H	104	68	150	h	h
9	9	011	TAB (horizontal tab)	41	29	051	)	)	73	49	111	I	I	105	69	151	i	i
10	A	012	LF (NL line feed, new line)	42	2A	052	*	*	74	4A	112	J	J	106	6A	152	j	j
11	B	013	VT (vertical tab)	43	2B	053	+	+	75	4B	113	K	K	107	6B	153	k	k
12	C	014	FF (NP form feed, new page)	44	2C	054	,	,	76	4C	114	L	L	108	6C	154	l	l
13	D	015	CR (carriage return)	45	2D	055	-	-	77	4D	115	M	M	109	6D	155	m	m
14	E	016	SO (shift out)	46	2E	056	.	.	78	4E	116	N	N	110	6E	156	n	n
15	F	017	SI (shift in)	47	2F	057	/	/	79	4F	117	O	O	111	6F	157	o	o
16	10	020	DLE (data link escape)	48	30	060	0	0	80	50	120	P	P	112	70	160	p	p
17	11	021	DC1 (device control 1)	49	31	061	1	1	81	51	121	Q	Q	113	71	161	q	q
18	12	022	DC2 (device control 2)	50	32	062	2	2	82	52	122	R	R	114	72	162	r	r
19	13	023	DC3 (device control 3)	51	33	063	3	3	83	53	123	S	S	115	73	163	s	s
20	14	024	DC4 (device control 4)	52	34	064	4	4	84	54	124	T	T	116	74	164	t	t
21	15	025	NAK (negative acknowledge)	53	35	065	5	5	85	55	125	U	U	117	75	165	u	u
22	16	026	SYN (synchronous idle)	54	36	066	6	6	86	56	126	V	V	118	76	166	v	v
23	17	027	ETB (end of trans. block)	55	37	067	7	7	87	57	127	W	W	119	77	167	w	w
24	18	030	CAN (cancel)	56	38	070	8	8	88	58	130	X	X	120	78	170	x	x
25	19	031	EM (end of medium)	57	39	071	9	9	89	59	131	Y	Y	121	79	171	y	y
26	1A	032	SUB (substitute)	58	3A	072	:	:	90	5A	132	Z	Z	122	7A	172	z	z
27	1B	033	ESC (escape)	59	3B	073	;	;	91	5B	133	[	[	123	7B	173	{	{
28	1C	034	FS (file separator)	60	3C	074	<	<	92	5C	134	\	\	124	7C	174	|	
29	1D	035	GS (group separator)	61	3D	075	=	=	93	5D	135	]	]	125	7D	175	}	}
30	1E	036	RS (record separator)	62	3E	076	>	>	94	5E	136	^	^	126	7E	176	~	~
31	1F	037	US (unit separator)	63	3F	077	?	?	95	5F	137	_	_	127	7F	177		DEL

Source: www.LookupTables.com

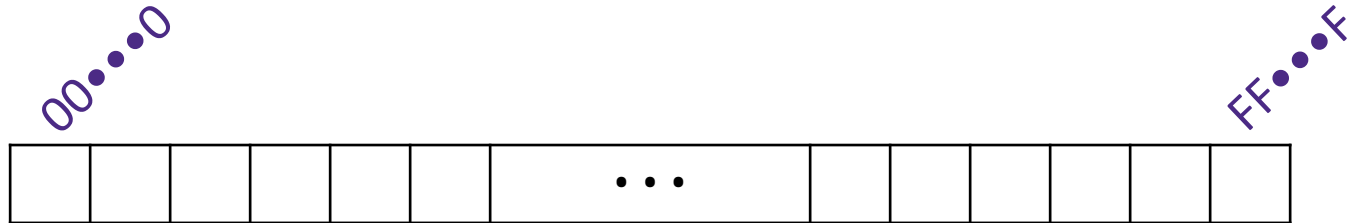
Memory, Data, & Addressing I

Binary Encoding Additional Details

- ❖ Because storage is finite in reality, everything is stored as “fixed” length
 - Data is moved and manipulated in fixed-length chunks
 - Multiple fixed lengths (*e.g.* 1 byte, 4 bytes, 8 bytes)
 - Leading zeros now *must* be included up to “fill out” the fixed length

- ❖ Example: the “eight-bit” representation of the number 4 is 0b00000100
 - Most Significant Bit (MSB)
 - Least Significant Bit (LSB)

Byte-Oriented Memory Organization



- ❖ Conceptually, memory is a single, large array of bytes, each with a unique *address* (index)
 - Each address is just a number represented in *fixed-length* binary
- ❖ Programs refer to bytes in memory by their *addresses*
 - Domain of possible addresses = *address space*
 - **Pointer: We can store addresses as data to “remember” where other data is in memory** **HIGH RISK AREA**
- ❖ But not all values fit in a single byte... (e.g. 295)
 - Many operations actually use multi-byte values

Peer Instruction Question

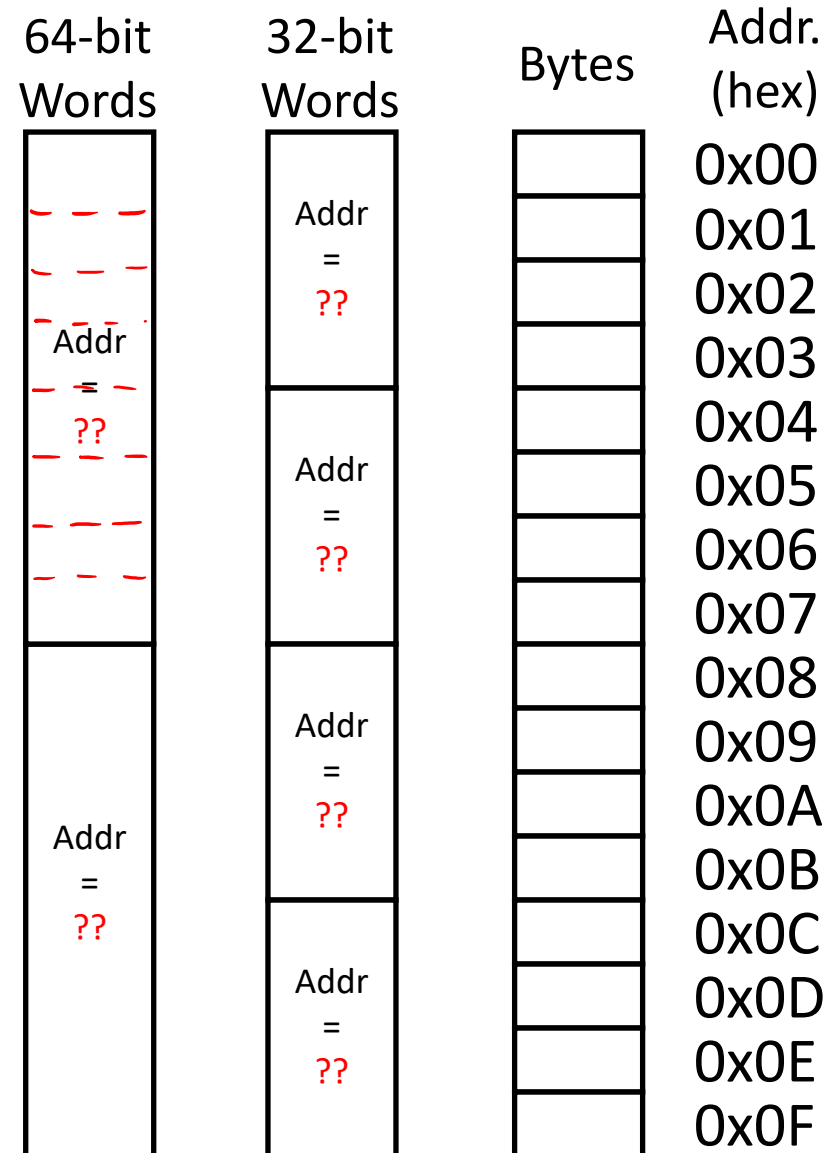
- ❖ If we choose to use 4-bit addresses, how big is our address space?
 - *i.e.* How much space can we “refer to” using our addresses?
- A. 16 bits
- B. 16 bytes
- C. 4 bits
- D. 4 bytes
- E. We're lost...

Machine “Words”

- ❖ We have *chosen* to tie word size to address size/width
 - word size = address size = register size
 - word size = w bits $\rightarrow 2^w$ addresses
- ❖ Current x86 systems use **64-bit (8-byte) words**
 - Potential address space: 2^{64} addresses
 2^{64} bytes $\approx$ **1.8×10^{19} bytes**
= 18 billion billion bytes = 18 EB (exabytes)
 - Actual physical address space: **48 bits**

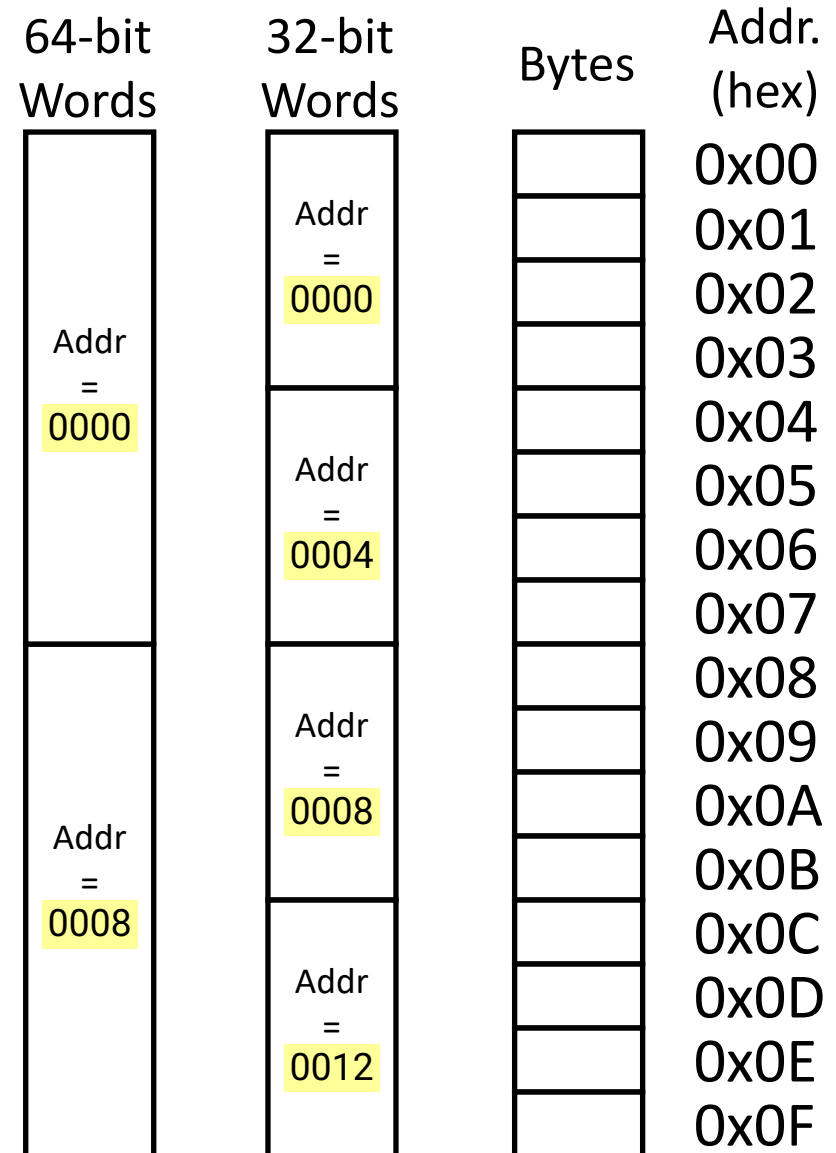
Word-Oriented Memory Organization

- ❖ Addresses still specify locations of *bytes* in memory
 - Addresses of successive words differ by word size (in bytes):
e.g. 4 (32-bit) or 8 (64-bit)
 - Address of word 0, 1, ... 10?



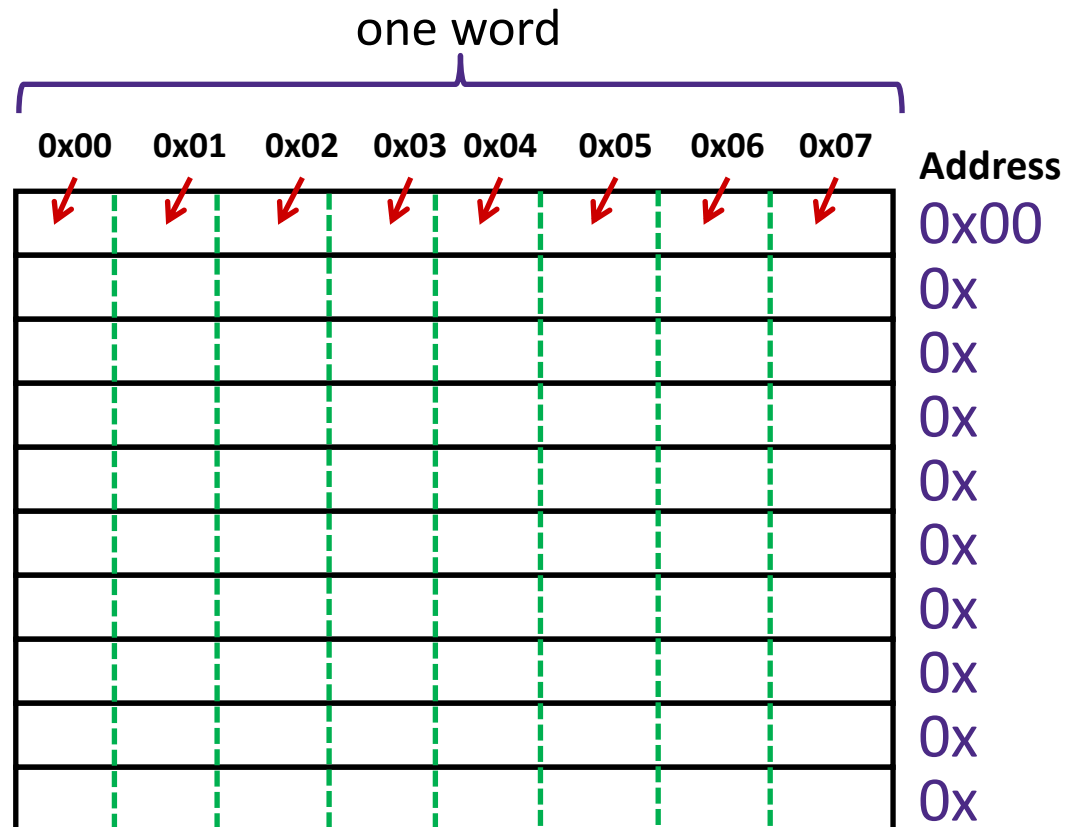
Word-Oriented Memory Organization

- ❖ Addresses still specify locations of *bytes* in memory
 - Addresses of successive words differ by word size (in bytes):
e.g. 4 (32-bit) or 8 (64-bit)
 - Address of word 0, 1, ... 10?
- ❖ **Address of word**
= address of *first* byte in word
 - The address of *any* chunk of memory is given by the address of the first byte
 - ***Alignment***



A Picture of Memory (64-bit view)

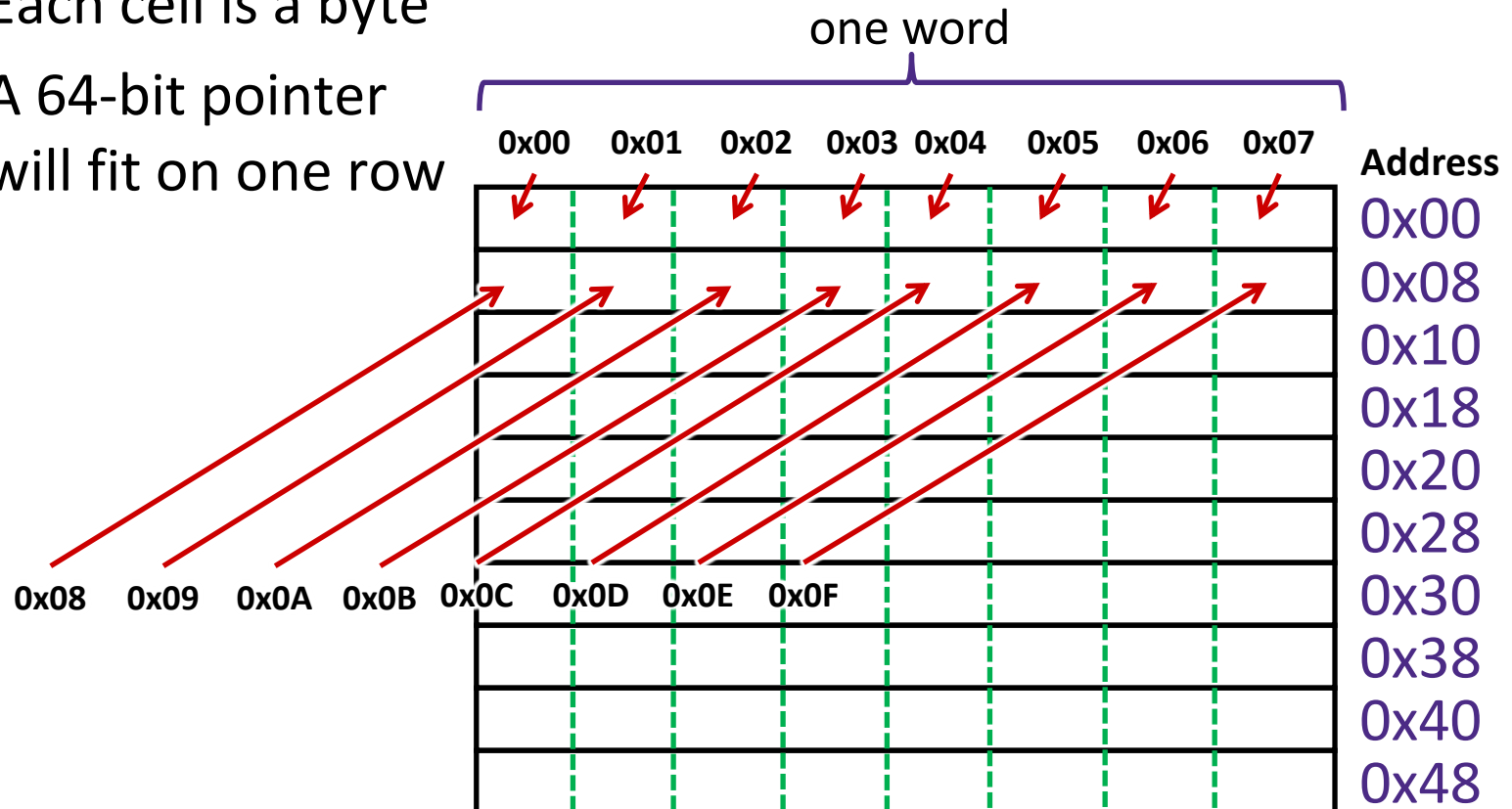
- ❖ A “64-bit (8-byte) word-aligned” view of memory:
 - In this type of picture, each row is composed of 8 bytes
 - Each cell is a byte
 - A 64-bit pointer will fit on one row



A Picture of Memory (64-bit view)

❖ A “64-bit (8-byte) word-aligned” view of memory:

- In this type of picture, each row is composed of 8 bytes
- Each cell is a byte
- A 64-bit pointer will fit on one row



Addresses and Pointers

64-bit example
(pointers are 64-bits wide)
big-endian

- ❖ An *address* is a location in memory
- ❖ A *pointer* is a data object that holds an address
 - Address can point to *any* data
- ❖ Value 504 stored at address **0x08**
 - $504_{10} = 1F8_{16}$
= 0x 00 ... 00 01 F8
- ❖ Pointer stored at **0x38** points to address **0x08**

Address	
0x00	
0x08	00 00 00 00 00 00 01 F8
0x10	
0x18	
0x20	
0x28	
0x30	
0x38	00 00 00 00 00 00 00 08
0x40	
0x48	

Addresses and Pointers

64-bit example
(pointers are 64-bits wide)

big-endian

- ❖ An *address* is a location in memory
- ❖ A *pointer* is a data object that holds an address
 - Address can point to *any* data
- ❖ Pointer stored at **0x48** points to address **0x38**
 - Pointer to a pointer!
- ❖ Is the data stored at **0x08** a pointer?
 - Could be, depending on how you use it

Address	
0x00	
0x08	00 00 00 00 00 00 01 F8
0x10	
0x18	
0x20	
0x28	
0x30	
0x38	00 00 00 00 00 00 00 08
0x40	
0x48	00 00 00 00 00 00 00 38



Data Representations

❖ Sizes of data types (in bytes)

Java Data Type	C Data Type	32-bit	x86-64
boolean	bool	1	1
byte	char	1	1
char		2	2
short	short int	2	2
int	int	4	4
float	float	4	4
	long int	4	8
double	double	8	8
long	long	8	8
	long double	8	16
(reference)	pointer *	4	8

address size = word size

To use "bool" in C, you must `#include <stdbool.h>`

Memory Alignment

- ❖ **Aligned:** Primitive object of K bytes must have an address that is a multiple of K
 - More about alignment later in the course

K	Type
1	char
2	short
4	int, float
8	long, double, pointers

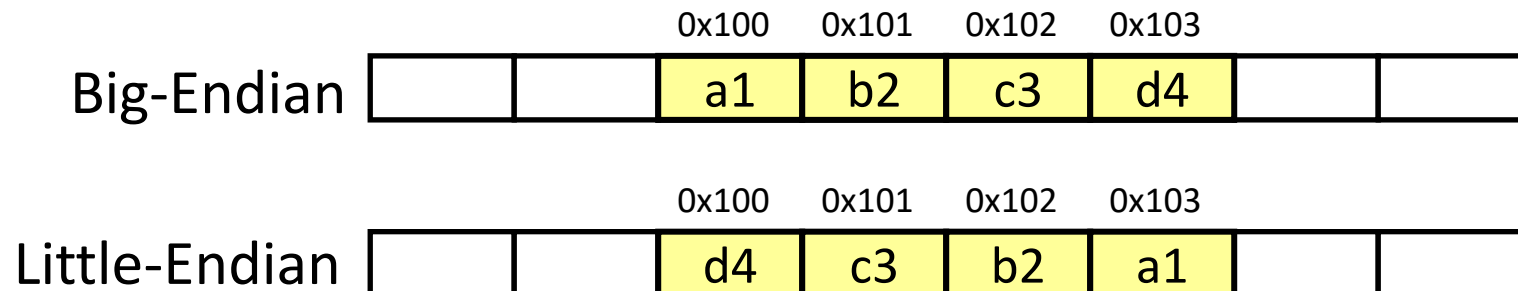
- ❖ For good memory system performance, data has to be aligned.

Byte Ordering

- ❖ How should bytes within a word be ordered *in memory*?
 - **Example:** store the 4-byte (32-bit) `int`:
0x a1 b2 c3 d4
- ❖ By convention, ordering of bytes called *endianness*
 - The two options are **big-endian** and **little-endian**
 - In which address does the least significant *byte* go?
 - Based on *Gulliver's Travels*: tribes cut eggs on different sides (big, little)

Byte Ordering

- ❖ Big-endian (SPARC, z/Architecture)
 - Least significant byte has highest address
- ❖ Little-endian (x86, x86-64, **RISC-V**)
 - Least significant byte has lowest address
- ❖ Bi-endian (ARM, PowerPC)
 - Endianness can be specified as big or little
- ❖ **Example:** 4-byte data 0xa1b2c3d4 at address 0x100



Memory, Data, & Addressing II

Review

- 1) If the word size of a machine is 64-bits, which of the following is usually true? (pick all that apply)
 - a) 64 bits is the size of a pointer
 - b) 64 bits is the size of an integer
 - c) 64 bits is the width of a register
- 2) (True/False) By looking at the bits stored in memory, I can tell if a particular 4-bytes is being used to represent an integer, floating point number, or instruction.
- 3) If the size of a pointer on a machine is 6 bits, the address space is how many bytes?

Assignment in C

32 bit example

(pointers are **32**-bits
wide)

& = "address of"

* = "dereference"

- ❖ left-hand side = right-hand side;
 - LHS must evaluate to a *location*
 - RHS must evaluate to a *value* (could be an address)
 - Store RHS value at LHS location

❖ **int** x, y;

❖ x = 0;

❖ y = 0x3CD02700;

❖ x = y + 3;

- Get value at y, add 3, store in x

❖ **int*** z = &y + 3;

- Get address of y, "add 3", store in z

	0x00	0x01	0x02	0x03	
0x00					
0x04	03	27	D0	3C	x
0x08					
0x0C					
0x10					
0x14					
0x18	00	27	D0	3C	y
0x1C					
0x20	24	00	00	00	z
0x24					

Pointer arithmetic

Pointer Arithmetic

- ❖ Pointer arithmetic is scaled by the size of target type
 - In this example, `sizeof(int) = 4`
- ❖ `int* z = &y + 3;`
 - Get address of `y`, add `3*sizeof(int)`, store in `z`
 - $\&y = 0x18 = 1*16^1 + 8*16^0 = 24$
 - $24 + 3*(4) = 36 = 2*16^1 + 4*16^0 = 0x24$
- ❖ **Pointer arithmetic can be dangerous!**
 - Can easily lead to bad memory accesses
 - Be careful with data types and *casting*

Assignment in C

- ❖ `int x, y;`
- ❖ `x = 0;`
- ❖ `y = 0x3CD02700;`
- ❖ `x = y + 3;`
 - Get value at `y`, add 3, store in `x`
- ❖ `int* z = &y + 3;`
 - Get address of `y`, add **12**, store in `z`
- ❖ `*z = y;`
 - What does this do?

32 bit example

(pointers are **32**-bits
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`&` = "address of"

`*` = "dereference"

	0x00	0x01	0x02	0x03	
0x00					
0x04	03	27	D0	3C	x
0x08					
0x0C					
0x10					
0x14					
0x18	00	27	D0	3C	y
0x1C					
0x20	24	00	00	00	z
0x24					

Assignment in C

32 bit example

(pointers are **32**-bits
wide)

& = "address of"

* = "dereference"

❖ `int x, y;`

❖ `x = 0;`

❖ `y = 0x3CD02700;`

❖ `x = y + 3;`

- Get value at `y`, add 3, store in `x`

❖ `int* z = &y + 3;`

- Get address of `y`, add **12**, store in `z`

The target of a pointer
is also a location

❖ `*z = y;`

- Get value of `y`, put in address
stored in `z`

	0x00	0x01	0x02	0x03	
0x00					
0x04	03	27	D0	3C	x
0x08					
0x0C					
0x10					
0x14					
0x18	00	27	D0	3C	y
0x1C					
0x20	24	00	00	00	z
0x24	00	27	D0	3C	

Arrays in C

Declaration: `int a[6];`

element type

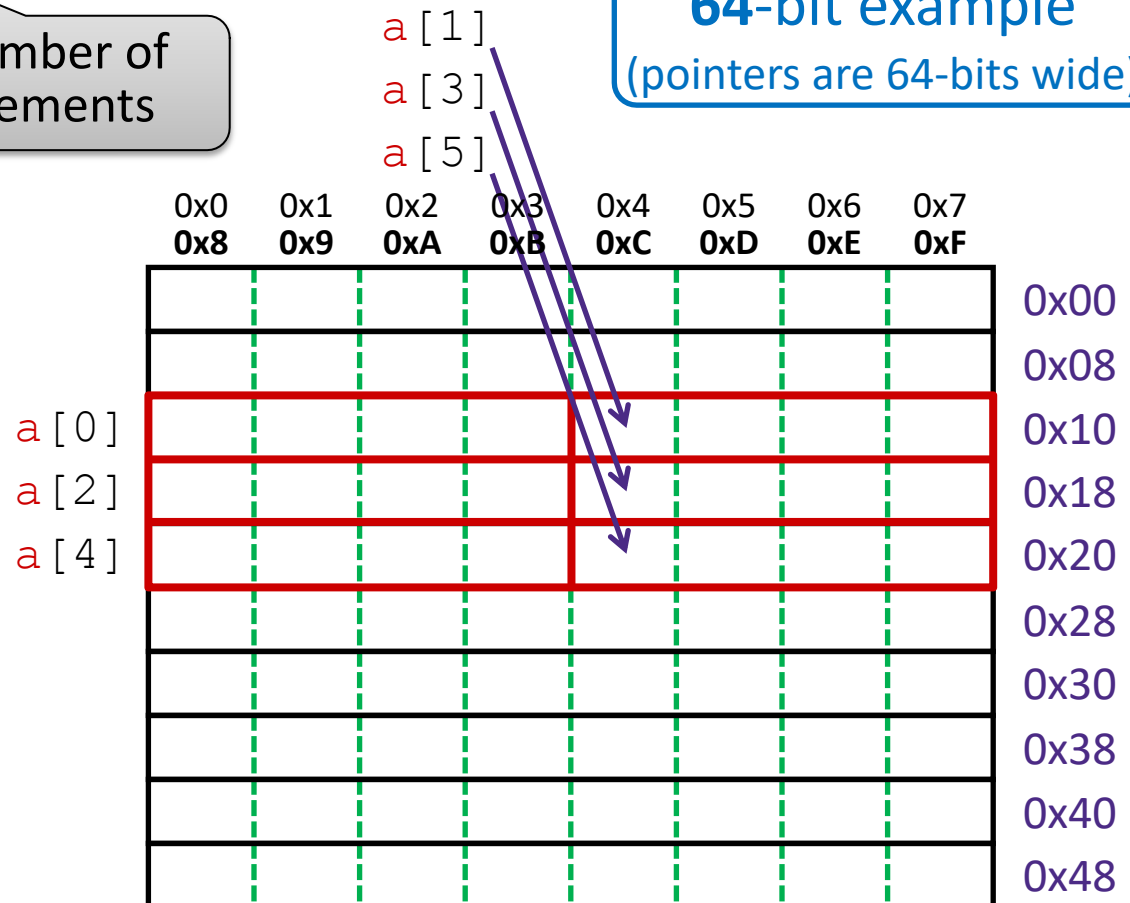
name

number of elements

Arrays are adjacent locations in memory storing the same type of data object

a (array name) returns the array's address

64-bit example
(pointers are 64-bits wide)



Arrays Basics

- **Pitfall:** An array in C does not know its own length, and its bounds are not checked!
 - We can accidentally access off the end of an array
 - We must pass the array **and its size** to any procedure that is going to manipulate it
- Mistakes with array bounds cause *segmentation faults* and *bus errors*
 - Be careful! These are VERY difficult to find (You'll learn how to debug these in lab)

Arrays in C

Declaration: `int a[6];`

Indexing: `a[0] = 0x015f;`
`a[5] = a[0];`

Arrays are adjacent locations in memory storing the same type of data object

a (array name) returns the array's address

&a[i] is the address of **a[0]** plus **i** times the element size in bytes

	0x0 0x8	0x1 0x9	0x2 0xA	0x3 0xB	0x4 0xC	0x5 0xD	0x6 0xE	0x7 0xF	
									0x00
									0x08
<code>a[0]</code>	5F	01	00	00					0x10
<code>a[2]</code>									0x18
<code>a[4]</code>					5F	01	00	00	0x20
									0x28
									0x30
									0x38
									0x40
									0x48

Arrays in C

Declaration: `int a[6];`

Indexing: `a[0] = 0x015f;`
`a[5] = a[0];`

No bounds checking: `a[6] = 0xBAD;`
`a[-1] = 0xBAD;`

Arrays are adjacent locations in memory storing the same type of data object

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`&a[i]` is the address of `a[0]` plus `i` times the element size in bytes

	0x0 0x8	0x1 0x9	0x2 0xA	0x3 0xB	0x4 0xC	0x5 0xD	0x6 0xE	0x7 0xF	
									0x00
					AD	0B	00	00	0x08
<code>a[0]</code>	5F	01	00	00					0x10
<code>a[2]</code>									0x18
<code>a[4]</code>					5F	01	00	00	0x20
	AD	0B	00	00					0x28
									0x30
									0x38
									0x40
									0x48

Arrays in C

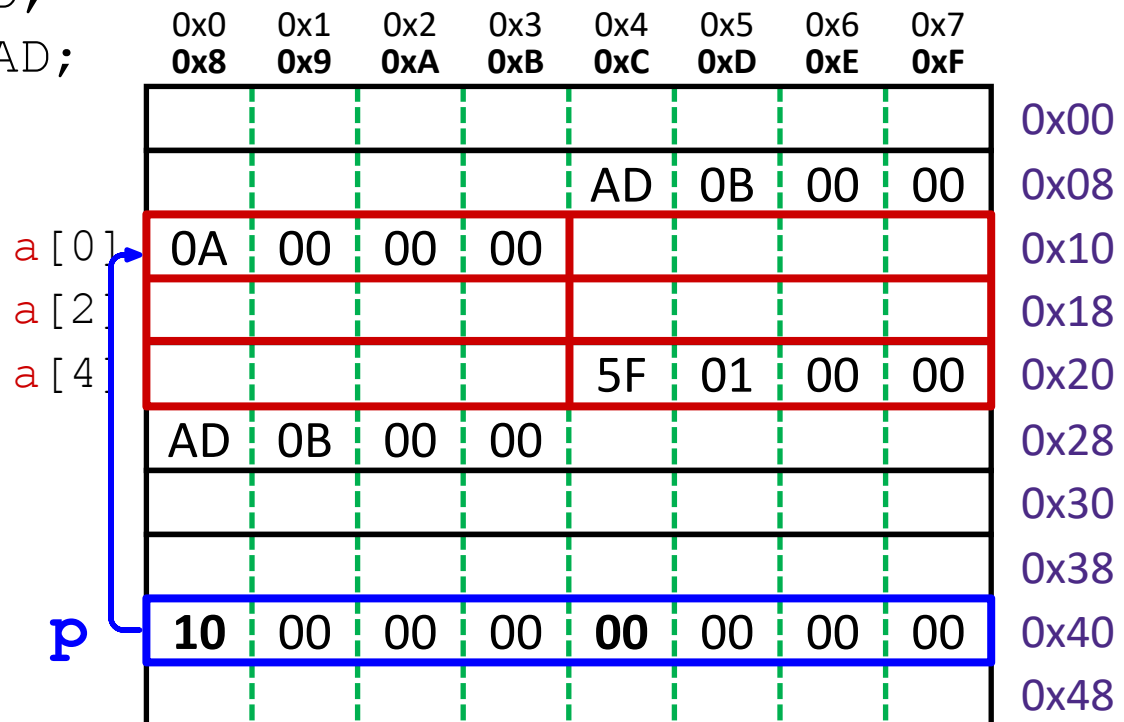
Declaration: `int a[6];`

Indexing: `a[0] = 0x015f;`
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Pointers: `int* p;`

equivalent $\left\{ \begin{array}{l} p = a; \\ p = \&a[0]; \\ *p = 0xA; \end{array} \right.$



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array indexing = address arithmetic
 (both scaled by the size of the type)

equivalent $\left\{ \begin{array}{l} p[1] = 0xB; \\ *(p+1) = 0xB; \\ p = p + 2; \end{array} \right.$

Arrays are adjacent locations in memory storing the same type of data object

a (array name) returns the array's address

$\&a[i]$ is the address of `a[0]` plus `i` times the element size in bytes

	0x0 0x8	0x1 0x9	0x2 0xA	0x3 0xB	0x4 0xC	0x5 0xD	0x6 0xE	0x7 0xF	
					AD	0B	00	00	0x00
$a[0]$	0A	00	00	00	0B	00	00	00	0x08
$a[2]$									0x10
$a[4]$					5F	01	00	00	0x18
	AD	0B	00	00					0x20
									0x28
									0x30
									0x38
p	10	00	00	00	00	00	00	00	0x40
									0x48

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equivalent $\left\{ \begin{array}{l} p[1] = 0xB; \\ *(p+1) = 0xB; \\ p = p + 2; \end{array} \right.$

`*p = a[1] + 1;`

Arrays are adjacent locations in memory storing the same type of data object

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`&a[i]` is the address of `a[0]` plus `i` times the element size in bytes

	0x0 0x8	0x1 0x9	0x2 0xA	0x3 0xB	0x4 0xC	0x5 0xD	0x6 0xE	0x7 0xF	
					AD	0B	00	00	0x00
									0x08
<code>a[0]</code>	0A	00	00	00	0B	00	00	00	0x10
<code>a[2]</code>	0C	00	00	00					0x18
<code>a[4]</code>					5F	01	00	00	0x20
	AD	0B	00	00					0x28
									0x30
									0x38
p	18	00	00	00	00	00	00	00	0x40
									0x48

Representing strings

- ❖ C-style string stored as an array of bytes (**char***)
 - Elements are one-byte **ASCII codes** for each character
 - No “String” keyword, unlike Java

32	space	48	0	64	@	80	P	96	`	112	p
33	!	49	1	65	A	81	Q	97	a	113	q
34	”	50	2	66	B	82	R	98	b	114	r
35	#	51	3	67	C	83	S	99	c	115	s
36	\$	52	4	68	D	84	T	100	d	116	t
37	%	53	5	69	E	85	U	101	e	117	u
38	&	54	6	70	F	86	V	102	f	118	v
39	'	55	7	71	G	87	W	103	g	119	w
40	(	56	8	72	H	88	X	104	h	120	x
41	)	57	9	73	I	89	Y	105	i	121	y
42	*	58	:	74	J	90	Z	106	j	122	z
43	+	59	;	75	K	91	[	107	k	123	{
44	,	60	<	76	L	92	\	108	l	124	
45	-	61	=	77	M	93	]	109	m	125	}
46	.	62	>	78	N	94	^	110	n	126	~
47	/	63	?	79	O	95	_	111	o	127	del

ASCII: American Standard Code for Information

Null-Terminated Strings

- ❖ **Example:** "Donald Trump" stored as a 13-byte array

<i>Decimal:</i>	68	111	110	97	108	100	32	84	114	117	109	112	0
<i>Hex:</i>	0x44	0x6F	0x6E	0x61	0x6C	0x64	0x20	0x54	0x72	0x75	0x6D	0x70	0x00
<i>Text:</i>	D	o	n	a	l	d		T	r	u	m	p	\0

- ❖ Last character followed by a 0 byte (' \0 ')
(a.k.a. "**null terminator**")
 - Must take into account when allocating space in memory
 - Note that ' 0 ' $\neq$ ' \0 ' (*i.e.* character 0 has non-zero value)
- ❖ How do we compute the length of a string?
 - Traverse array until null terminator encountered

C (char = 1 byte)

Endianness and Strings

```
char s[6] = "12345";
```

String literal

0x31 = 49 decimal = ASCII '1'

IA32, x86-64
(little-endian)

SPARC
(big-endian)

0x00	31	↔	31	0x00	'1'
0x01	32	↔	32	0x01	'2'
0x02	33	↔	33	0x02	'3'
0x03	34	↔	34	0x03	'4'
0x04	35	↔	35	0x04	'5'
0x05	00	↔	00	0x05	'\0'

- ❖ Byte ordering (endianness) is not an issue for 1-byte values
 - The whole array does not constitute a single value
 - Individual elements are values; chars are single bytes

Examining Data Representations

❖ Code to print byte representation of data

- Any data type can be treated as a *byte array* by **casting** it to `char`
- C has **unchecked** casts **!! DANGER !!**

```
void show_bytes(char* start, int len) {  
    int i;  
    for (i = 0; i < len; i++)  
        printf("%p\t0x%.2x\n", start+i, *(start+i));  
    printf("\n");  
}
```

printf directives:

<code>%p</code>	Print pointer
<code>\t</code>	Tab
<code>%x</code>	Print value as hex
<code>\n</code>	New line

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        printf("%p\t0x%.2x\n", start+i, *(start+i));  
    printf("\n");  
}
```

```
void show_int(int x) {  
    show_bytes( (char *) &x, sizeof(int));  
}
```

show_bytes Execution Example

```
int x = 12345; // 0x00003039
printf("int x = %d;\n", x);
show_int(x); // show_bytes((char *) &x,
sizeof(int));
```

❖ Result (Linux x86-64):

- **Note:** The addresses will change on each run (try it!), but fall in same general range

```
int x = 12345;
0x7fffb7f71dbc 0x39
0x7fffb7f71dbd 0x30
0x7fffb7f71dbe 0x00
```