Work Distribution and Scheduling
Programming for high performance

- Optimizing the performance of parallel programs is an iterative process of refining choices for decomposition, assignment, and orchestration...

- Key goals (that are at odds with each other)
  - Balance workload onto available execution resources
  - Reduce communication (to avoid stalls)
    - Reduce extra work (overhead) performed to increase parallelism, manage assignment, reduce communication, etc.

- We are going to talk about a rich space of techniques
TIP #1: Always implement the simplest solution first, then measure performance to determine if you need to do better.

(Example: if you anticipate only running low-core count machines, it may be unnecessary to implement a complex approach that creates and hundreds or thousands of pieces of independent work)
Balancing the workload

Ideally: all processors are computing all the time during program execution (they are computing simultaneously, and they finish their portion of the work at the same time)

Recall Amdahl’s Law:
Only small amount of load imbalance can significantly bound maximum speedup

P4 does 20% more work → P4 takes 20% longer to complete

→ 20% of parallel program’s runtime is serial execution

(work in serialized section here is about 5% of the work of the entire program: S=.05 in Amdahl’s law equation)
Static assignment

- Assignment of work to threads is written into the program
  - Not necessarily determined at compile-time (assignment algorithm may depend on runtime parameters such as input, threads)
- Recall solver example: assign equal number of grid cells (work) to each thread (worker)
When is static assignment applicable?

- When the cost (execution time) of work and the amount of work is **predictable** (so the programmer can work out a good assignment in advance)

- Simplest example: it is known up front that all work has the same cost

In the example above:
There are 12 tasks, and it is known that each have the same cost.
Assignment solution: statically assign three tasks to each of the four processors.
When is static assignment applicable?

- When work is predictable, but not all jobs have the same cost
- When statistics about execution time are known (e.g., same cost)

Jobs have unequal, but known cost: assign to processors to ensure overall good load balance.
“Semi-static” assignment

- Cost of work is predictable for near-term future
  - Idea: recent past is a good predictor of near future
- Application periodically profiles application and re-adjusts assignment
  - Assignment is “static” for the interval between re-adjustments

Particle simulation:
Redistribute particles as they move over course of simulation
(if motion is slow, redistribution need not occur often)

Adaptive mesh:
Mesh is changed as object moves or flow over object changes, but changes occur slowly (color indicates assignment of parts of mesh to processors)
Dynamic assignment

Program determines assignment dynamically at runtime to ensure a well-distributed load. (The execution time of tasks, or the total number of tasks, is unpredictable.)

### Sequential program (independent loop iterations)

```c
int N = 1024;
int* x = new int[N];
bool* prime = new bool[N];

// assume elements of x initialized
for (int i=0; i<N; i++)
{
    // unknown execution time
    is_prime[i] = test_primality(x[i]);
}
```

### Parallel program (SPMD execution by multiple threads, shared address space model)

```c
int N = 1024;
// assume allocations are only executed by 1 thread
int* x = new int[N];
bool* is_prime = new bool[N];
// assume elements of x are initialized here
LOCK counter_lock;
int counter = 0;  // shared variable

while (1) {
    int i;
    lock(counter_lock);
    i = counter++
    atomic_incr(counter);
    unlock(counter_lock);
    if (i >= N)
        break;
    is_prime[i] = test_primality(x[i]);
}
```
Dynamic assignment using a work queue

Sub-problems (a.k.a. “tasks”, “work”)

Shared work queue: a list of work to do (for now, let’s assume each piece of work is independent)

Worker threads:
Pull data from shared work queue
Push new work to queue as it is created
What constitutes a piece of work? What is a potential problem with this design?

```cpp
const int N = 1024;

// assume allocations are only executed by 1 thread
float* x = new float[N];  bool*
prime = new bool[N];

// assume elements of x are initialized here
LOCK counter_lock;  int
counter = 0;

while (1) {  int i;
    lock(counter_lock); i =
    counter++;;
    unlock(counter_lock); if (i
    >= N)
        break;
    is_prime[i] = test_primality(x[i]);
}
```

Fine granularity partitioning: 1 “task” = 1 element

Likely good workload balance (many small tasks) Potential for high synchronization cost (serialization at critical section)

So... IS IT a problem?

Time in task 0

Time in critical section

This is overhead that does not exist in serial program

And.. it’s serial execution (recall Amdahl’s Law)
Increasing task granularity

const int N = 1024;
const int GRANULARITY = 10;

// assume allocations are only executed by 1 thread
float* x = new float[N]; bool*
prime = new bool[N];
// assume elements of x are initialized here

LOCK counter_lock;
int counter = 0;

while (1) { int
i;
lock(counter_lock); i =
counter;
counter += GRANULARITY;
unlock(counter_lock); if (i
>= N)
break;
int end = min(i + GRANULARITY, N); for
(int j=i; j<end; j++)
is_prime[i] = test_primality(x[j]);
}

Coarse granularity partitioning: 1 “task” = 10 elements Decreased synchronization
(Critical section entered 10 times less)
Choosing task size

- Useful to have many more tasks* than processors
  (many small tasks enables good workload balance via dynamic assignment)
  - Motivates small granularity tasks

- But want as few tasks as possible to minimize overhead of managing the assignment
  - Motivates large granularity tasks

- Ideal granularity depends on many factors
  (Common theme in this course: must know your workload, and your machine)

*I had to pick a term for a piece of work, a sub-problem, etc.*
Smarter task scheduling

Consider dynamic scheduling via a shared work queue

What happens if the system assigns these tasks to workers in left-to-right order?
Smarter task scheduling

What happens if scheduler runs the long task last? Potential for load imbalance!

One possible solution to imbalance problem:

Divide work into a larger number of smaller tasks
  - Hopefully “long pole” gets shorter relative to overall execution time
  - May increase synchronization overhead
  - May not be possible (perhaps long task is fundamentally sequential)
Smarter task scheduling

Schedule long task first to reduce “slop” at end of computation

Another solution: smarter
Schedule long tasks first

- Thread performing long task performs fewer overall tasks, but approximately the same amount of work as the other threads.
- Requires some knowledge of workload (some predictability of cost)
Decreasing synchronization overhead using a distributed set of queues
(avoid need for all workers to synchronize on single work queue)

Subproblems (a.k.a. “tasks”, “work to do”)

Set of work queues
(In general, one per worker thread)

Worker threads:
Pull data from OWN work queue Push new work to OWN work queue
When local work queue is empty...
STEAL work from another work queue
Work in task queues need not be independent

A task is not removed from queue and assigned to worker thread until all task dependencies are satisfied

Workers can submit new tasks (with optional explicit dependencies) to task system

```c
foo_handle = enqueue_task(foo); // enqueue task foo (independent of all prior tasks)
bar_handle = enqueue_task(bar, foo_handle); // enqueue task bar, cannot run until foo is complete
```
Challenge: achieving good workload balance
- Want all processors working all the time
- But want low-cost solution for achieving this balance
  - Minimize computational overhead
  - Minimize synchronization costs

Static assignment vs. dynamic assignment
- Really, it is not an either/or decision, Use up-front knowledge about workload as much as possible to reduce load imbalance and task management/synchronization costs (in the limit, if the system knows everything, use fully static assignment)

Issues discussed today span aspects of task decomposition, assignment, and orchestration
Scheduling fork-join parallelism
Common parallel programming patterns

Data parallelism:
Perform same sequence of operations on many data elements

// ISPC foreach
foreach (i=0 ... N) {
    B[i] = foo(A[i]);
}

// ISPC bulk task launch
launch[numTasks] myFooTask(A, B);

// using higher-order function ‘map’
map(foo, A, B);

// openMP parallel for
#pragma omp parallel for
for (int i=0; i<N; i++) {
    B[i] = foo(A[i]);
}

// bulk CUDA thread launch (GPU programming)
foo<<<numBlocks, threadsPerBlock>>>(A, B);
Common parallel programming patterns

Explicit management of parallelism with threads:
Create one thread per execution unit (or per amount of
desired concurrency)
   - Example below: C code with C++ threads

```cpp
float* A;
float* B;

// initialize A and B std::thread
thread[MAX_THREADS];

for (int i=0; i<num_cores; i++) {
    thread[i] = std::thread(myFunction, A, B);
}

for (int i=0; i<num_cores; i++)
    { thread[i].join();
}
```
Consider divide-and-conquer algorithms

**Quick sort:**

```c
// sort elements from ‘begin’ up to (but not including) ‘end’
void quick_sort(int* begin, int* end) {
    if (begin >= end-1)
        return;
    else {
        int* middle = partition(begin, end);
        quick_sort(begin, middle);
        quick_sort(middle+1, last);
    }
}
```

Dependences

![Diagram showing dependencies between quick_sort functions](dependencies_diagram)
Fork-join pattern

- Natural way to express independent work inherent in divide-and-conquer algorithms
- This lecture’s code examples will be in Cilk Plus
  - C++ language extension
  - Originally developed at MIT, now adapted as open standard (in GCC, Intel ICC)

```cilk
  cilk_spawn foo(args);
```

“fork” (create new logical thread)

Semantics: invoke foo, but unlike standard function call, caller may continue executing asynchronously with execution of foo.

```cilk
  cilk_sync;
```

“join”

Semantics: returns when all calls spawned by current function have completed. (“sync up” with the spawned calls)
Call-return of a C function

```c
void my_func() {
    // calling function (part A)
    foo();
    bar();
    // calling function (part B)
}
```

Semantics of a function call:
Control moves to the function that is called
(Thread executes instructions for the function)

When function returns, control returns back to caller (thread resumes executing instructions from the caller)
Basic Cilk Plus examples

// foo() and bar() may run in parallel
cilk_spawn foo();
bar();
cilk_sync;

Same amount of independent work first example, but potentially higher runtime overhead (due to two spawns vs. one)

// foo, bar, fizz, buzz, may run in parallel

cilk_spawn foo();
cilk_spawn bar();
cilk_spawn fizz();
buzz();
cilk_sync;
Abstraction vs. implementation

- Notice that the `cilk_spawn` abstraction does not specify how or when spawned calls are scheduled
  - Only that they may be run concurrently with caller (and with all other calls spawned by the caller)

- But `cilk_sync` does serve as a constraint on scheduling
  - All spawned calls must complete before `cilk_sync` returns
void quick_sort(int* begin, int* end) {
  if (begin >= end - PARALLEL_CUTOFF)
    std::sort(begin, end);
  else {
    int* middle = partition(begin, end);
    cilk_spawn quick_sort(begin, middle);
    quick_sort(middle+1, last);
  }
}

Sort sequentially if problem size is sufficiently small (overhead of spawn trumps benefits of potential parallelization)
Writing fork-join programs

- Main idea: expose independent work (potential parallelism) to the system using `cilk_spawn`

- Recall parallel programming rules of thumb
  - Want at least as much work as parallel execution capability
  - Want more independent work than execution capability to allow for good workload balance
  - “parallel slack” = ratio of independent work to machine’s parallel execution capability (in practice: ~8 is a good ratio)
  - But not too much independent work so that granularity of work is too small (too much slack incurs overhead of managing fine-grained work)
Scheduling fork-join programs

- Consider very simple scheduler:
  - Launch pthread for each cilk_spawn using pthread_create
  - Translate cilk_sync into appropriate pthread_join calls

- Potential performance problems?
  - Heavyweight spawn operation
  - Many more concurrently running threads than cores
    - Context switching overhead
  - Larger working set than necessary, less cache locality
Pool of worker threads

- The Cilk Plus runtime maintains pool of threads
  - Think: all threads created at application launch *
  - Exactly as many worker threads as execution contexts

Example: Eight thread worker pool for my quad-core laptop with Hyper-Threading

```c
while (work_exists()) {  
    work = get_new_work();  
    work.run();  
}
```

* It’s perfectly fine to think about it this way, but in reality, runtimes tend to be lazy and initialize worker threads on the first Cilk spawn. (This is a common implementation strategy, ISPC does the same with worker threads that run ISPC tasks.)
Consider execution of the following code
Specifically, consider execution from the point `foo()` is spawned

cilk_spawn foo();
bar();
cilk_sync;

What threads should `foo()` and `bar()` be executed by?

Thread 0

Thread 1
First, consider a serial implementation

Run child first... via a regular function call
- Thread runs `foo()`, then returns from `foo()`, then runs `bar()`
- Continuation is implicit in the thread's stack

```
Executing `foo()`...
```

```
Traditional thread call stack (indicates `bar` will be performed next after return)
```

```
What if, while executing `foo()`, thread 1 goes idle...
```

```
Inefficient: thread 1 could be performing `bar()` at this time!
```
Per-thread work queues store “work to do”

Upon reaching `cilk_spawn foo()`, thread places continuation in its work queue, and begins executing `foo()`.

```
Thread 0 work queue

bar()

Empty!

Thread 1 work queue

Executing foo()…
```
Idle threads “steal” work from busy threads

If thread 1 goes idle (a.k.a. there is no work in its own queue), then it looks in thread 0’s queue for work to do.

1. Idle thread looks in busy thread’s queue for work
Idle threads “steal” work from busy threads

If thread 1 goes idle (a.k.a. there is no work in its own queue), then it looks in thread 0's queue for work to do.

1. Idle thread looks in busy threads queue for work

2. Idle thread moves work from busy thread's queue to its own queue

Executing foo()…
Idle threads “steal” work from busy threads

If thread 1 goes idle (a.k.a. there is no work in its own queue), then it looks in thread 0’s queue for work to do.

1. Idle thread looks in busy threads queue for work.
2. Idle thread moves work from busy thread’s queue to its own queue.
3. Thread resumes execution.

Executing foo()…

Executing bar()…
At spawn, should thread run child or continuation?

```
cilk_spawn foo();
bar();
cilk_sync;
```

Run continuation first: record child for later execution
- Child is made available for stealing by other threads (“child stealing”)

Run child first: record continuation for later execution
- Continuation is made available for stealing by other threads (“continuation stealing”)

Which implementation do we choose?
Consider thread executing the following code

```c
for (int i=0; i<N; i++) {
    cilk_spawn foo(i);
}
cilk_sync;
```

- **Run continuation first (“child stealing”)**
  - Caller thread spawns work for all iterations before executing any of it
  - Think: breadth-first traversal of call graph. \(O(N)\) space for spawned work (maximum space)
  - If no stealing, execution order is very different than that of program with `cilk_spawn` removed
for (int i=0; i<N; i++) {
    cilk_spawn foo(i);
}
cilk_sync;

Run child first (“continuation stealing”)
- Caller thread only creates one item to steal
  (continuation that represents all remaining iterations)
- If no stealing occurs, thread continually pops
  continuation from work queue, enqueues new
  continuation (with updated value of i)
- Order of execution is the same as for program with
  spawn removed.
- Think: depth-first traversal of call graph
Consider thread executing the following code

```c
for (int i=0; i<N; i++) {
    cilk_spawn foo(i);
}
cilk_sync;
```

- **Run child first ("continuation stealing")**
  - Enqueues continuation with i advanced by 1
  - If continuation is stolen, stealing thread spawns and executes next iteration
  - Can prove that work queue storage for system with T threads is no more than T times that of stack storage for single threaded execution
Scheduling quicksort: assume 200 elements

void quick_sort(int* begin, int* end) {
  if (begin >= end - PARALLEL_CUTOFF)
    std::sort(begin, end);
  else {
    int* middle = partition(begin, end);
    cilk_spawn quick_sort(begin, middle);
    quick_sort(middle+1, last);
  }
}

What work in the queue should other threads steal?
(e.g., steal from top or bottom)

Thread 0 work queue  Thread 1 work queue

| cont: 101-200 |
| cont: 51-100  |
| cont: 26-50   |

Thread 2 work queue

Working on 0-25...
Implementing work stealing: dequeue per worker

Work queue implemented as a dequeue (double ended queue)
- Local thread pushes/pops from the “tail” (bottom)
- Remote threads steal from “head” (top)

- Th 0 work queue
  - cont: 26-50
  - Steal!

- Th 1 work queue
  - cont: 101-200

- Th 2 work queue
  - cont: 51-100
  - Steal!

...
Implementing work stealing: dequeue per worker

Work queue implemented as a dequeue (double ended queue)
- Local thread pushes/pops from the “tail” (bottom)
- Remote threads steal from “head” (top)

Thread 0 work queue

Thread 1 work queue

Thread 2 work queue

Working on 0-25…  Working on 101-150…  Working on 51-75…
Implementing work stealing: dequeue per worker

Work queue implemented as a dequeue (double ended queue)
- Local thread pushes/pops from the “tail” (bottom)
- Remote threads steal from “head” (top)

<table>
<thead>
<tr>
<th>Thread 0 work queue</th>
<th>Thread 1 work queue</th>
<th>Thread 2 work queue</th>
</tr>
</thead>
<tbody>
<tr>
<td>cont: 26-50</td>
<td>cont: 151-200</td>
<td>cont: 76-100</td>
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<tr>
<td>cont: 13-25</td>
<td>cont: 126-150</td>
<td>cont: 64-75</td>
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<td>cont: 114-125</td>
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</tr>
<tr>
<td>Working on 0-12…</td>
<td>Working on 101-113…</td>
<td>Working on 51-63…</td>
</tr>
</tbody>
</table>
Implementing work stealing: choice of victim

- Idle threads randomly choose a thread to steal from
- Steal work from top of dequeue:
  - Steals largest amount of work (reduce number of steals)
  - Maximum locality in work each thread performs (when combined with run child first scheme)
  - Stealing thread and local thread do not contend for same elements of dequeue (efficient lock-free implementations of dequeue exist)
Child-first work stealing scheduler anticipates divide-and-conquer parallelism

```c
void recursive_for(int start, int end) {
    while (start <= end - GRANULARITY) {
        int mid = (end - start) / 2;
        cilk_spawn recursive_for(start, mid);
        start = mid;
    }
    for (int i=start; i<end; i++) foo(i);
}
recursive_for(0, N);
```

for (int i=0; i<N; i++) {
    cilk_spawn foo(i);
}
cilk_sync;

Code at right generates work in parallel, (code at left does not), so it more quickly fills parallel machine
Implementing sync

for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}
cilk_sync;
bar();
Implementing sync: no stealing case

block (id: A)

for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}

cilk_sync; Sync for all calls spawned within block A

bar();

Thread 0 work queue  Thread 1 work queue

cont: i=10 (id=A)

If no work has been stolen by other threads, then there's nothing to do at the sync point.

cilk_sync is a no-op.

Working on foo(9), id=A…
Implementing sync: stalling join

```
block (id: A)
for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}
cilk_sync; Sync for all calls spawned within block A
bar();
```

Example 1: “stalling” join policy
Thread that initiates the fork must perform the sync.
Therefore it waits for all spawned work to be complete. In this case, thread 0 is the thread initiating the fork.
Implementing sync: stalling join

```c
for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}

cilk_sync; Sync for all calls spawned within block A

bar();
```

Idle thread 1 steals from busy thread 0

Note: descriptor for block A created

The descriptor tracks the number of outstanding spawns for the block, and the number of those spawns that have completed.

The 1 spawn tracked by the descriptor corresponds to foo(0) being run by thread 0. (Since the continuation is now owned by thread 1 after the steal.)
Implementing sync: stalling join

```c
block (id: A)
for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}
cilk_sync; Sync for all calls spawned within block A
bar();
```

Thread 0 work queue
```
| spawn: 2, done: 0 |
| id=A |
```

Thread 1 work queue
```
| cont: i=1, id=A |
| STOLEN (id=A) |
```

Thread 1 is now running foo(1)
Note: spawn count is now 2

Working on foo(0), id=A...

Working on foo(1), id=A...
Implementing sync: stalling join

block (id: A)

for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}

cilk_sync; Sync for all calls spawned within block A

bar();
Implementing sync: stalling join

block (id: A)
for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}
cilk_sync; Sync for all calls spawned within block A
bar();

Thread 0 work queue  Thread 1 work queue  Thread 2 work queue

<table>
<thead>
<tr>
<th>id=spawn:10, done:9</th>
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<tbody>
<tr>
<td>STOLEN (id=A)</td>
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Computation nearing end…
Only foo(9) remains to be completed.
Implementing sync: stalling join

block (id: A)
for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}
cilk_sync; **Sync for all calls spawned within block A**
bar();

```
for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}
cilk_sync;
```

Thread 0 work queue  Thread 1 work queue  Thread 2 work queue

**Last spawn completes.**
Implementing sync: stalling join

block (id: A)

for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}

cilk_sync; Sync for all calls spawned within block A

bar();

Thread 0 work queue  Thread 1 work queue  Thread 2 work queue

Thread 0 now resumes continuation and executes bar()  
Note block A descriptor is now free.

Working on bar()...  Idle!  Idle!
Implementing sync: greedy policy

block (id: A)

for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}

cilk_sync; **Sync for all calls spawned within block A**

bar();

---

Example 2: “greedy” policy

- When thread that initiates the fork goes idle, it looks to steal new work
- Last thread to reach the join point continues execution after sync
Implementing sync: greedy policy

```c
for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}
cilk_sync; /* Sync for all calls spawned within block A */
bar();
```

Block (id: A)

Idle thread 1 steals from busy thread 0 (as in the previous case)
Implementing sync: greedy policy

block (id: A)

for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}

cilk_sync;  Sync for all calls spawned within block A

bar();

Thread 0 work
queue

Thread 1 work
queue

Thread 0 completes foo(0)
No work to do in local dequeue, so thread 0 looks to steal!
Implementing sync: greedy policy

block (id: A)

for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}

cilk_sync; \textit{Sync for all calls spawned within block A}

bar();

Thread 0 work queue
id=3, spawn: 3, done: 1
cont: i=2, id=A

Thread 1 work queue
STOLEN (id=A)

Stea

Thread 0 now working on foo(2)

Working on foo(2), id=A...

Working on foo(1), id=A...
Implementing sync: greedy policy

```c
for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}
cilk_sync; \textit{Sync for all calls spawned within block A}
bar();
```

Assume thread 1 is the last to finish spawned calls for block A.
Implementing sync: greedy policy

```plaintext
block (id: A)
for (int i=0; i<10; i++) {
    cilk_spawn foo(i);
}
cilk_sync; Sync for all calls spawned within block A
bar();
```

Thread 0 work queue
Thread 1 work queue

Thread 1 continues on to run bar() Note block A descriptor is now free.
Cilk uses greedy join scheduling

- **Greedy join scheduling policy**
  - All threads always attempt to steal if there is nothing to do (threads only go idle if there is no work to steal in the system)
  - Worker thread that initiated spawn may not be thread that executes logic after `cilk_sync`

- **Remember:**
  - Overhead of bookkeeping steals and managing sync points only occurs when steals occur
  - If large pieces of work are stolen, this should occur infrequently
    - Most of the time, threads are pushing/popping local work from their local dequeue
Cilk summary

- **Fork-join parallelism: a natural way to express divide-and-conquer algorithms**
  - Discussed Cilk Plus, but many other systems also have fork/join primitives
  - e.g., OpenMP

- **Cilk Plus runtime implements spawn-sync abstraction with a locality-aware work stealing scheduler**
  - Always run spawned child (continuation stealing)
  - Greedy behavior at join (threads do not wait at join, immediately look for other work to steal)