

$AG(n \rightarrow EXt)$

is not expressible in LTL

Proof: Sup. it is expr. in LTL
by some formula φ

then

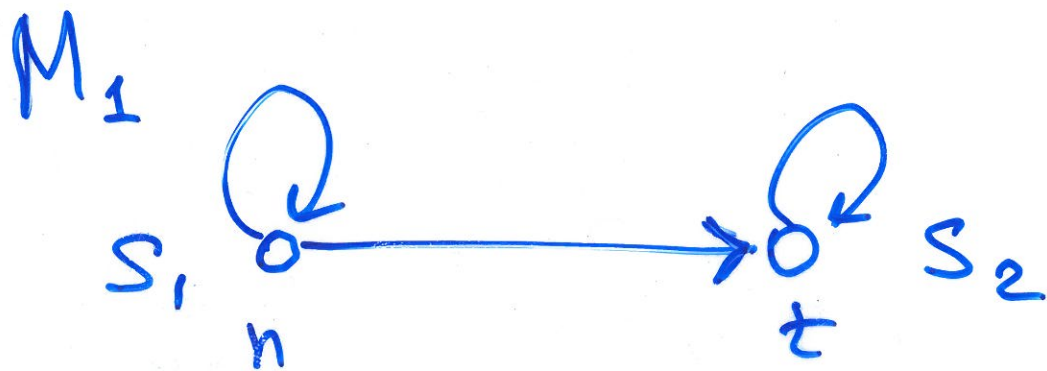
$$AG(n \rightarrow EXt) \equiv_{CTL^*} A[\varphi]$$

$\Downarrow$ def. $\equiv$

$\forall M \forall s$

$$\left(\begin{array}{l} M, s \models AG(n \rightarrow EXt) \\ \text{iff} \\ M, s \models A[\varphi] \end{array} \right)$$

In particular,



Since $M_1, s_1 \models AG(h \rightarrow EXt)$,
we have

$$M_1, s_1 \models A[\psi]$$

Consider M_2 :

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graph LR; start(( )) --> s1(((s1))); s1 -- h --> s1;
```

Since $M_1, s_1 \models A[\psi]$, we
must have $M_2, s_1 \models A[\psi]$

But $M_2, s_1 \not\models AG(h \rightarrow EXt)$!

Contradiction.